

Lessons 1-3 – *How Long is a Day?*

Open the GeoGebra app on your desktop and <https://www.geogebra.org/m/a4v7fzkt>

Day Length Formula

1. Go to the *Frames of Reference* chapter in the link
2. Open *Sun Always to the Right*
3. Watch the animation – what features do you notice?
 - a. Is the rate of movement constant? Where might you have seen this type of motion before?
 - b. What are the extremes of motion?
4. Pause the animation and experiment with the slider for yourself...
5. Have a go at the following questions:
 - a. In what frame of reference does this happen (what doesn't move)?
 - b. What does T represent in this diagram? What does its start value represent?
 - c. What is a "solar zenith locus"?
 - d. What do the arrows mean?
 - e. The Tropic of Cancer is at approximately 23.5° latitude
 - i. What latitude is the Tropic of Capricorn at?
 - ii. How are the tropics defined?
 - f. How are the polar (Arctic and Antarctic) circles defined?
 - i. What are their latitudes?
 - g. The longest day of the year occurs on Summer Solstice; the shortest on Winter Solstice. In the Northern hemisphere, Summer Solstice is around 21st June every year.
 - i. When is Winter Solstice in the Northern hemisphere?
 1. What is the value of T at that time?
 - ii. When do you think the Vernal (spring) Equinox and Autumnal Equinox are?
 1. What are the values of T at those times?
 - h. Now select the correct value of T to show each of:
 - i. Summer solstice in the Northern hemisphere
 - ii. Winter solstice in the Northern hemisphere
 - iii. Winter solstice in the Southern hemisphere
 - iv. Vernal Equinox
 - v. Autumnal Equinox
6. Now consider switching to a frame of reference in which the polar axis does not move...open *Polar Axis Frames*
 - a. What is meant by "High Noon"?
 - b. What could the moving brown dot represent?

- c. What does the darkened region represent?
 - d. What is the common name for α ?
 - e. Play the animation for T (at the same time) – compare the view on the left-hand side with that of the last applet...how do they differ?
 - f. Look at the compass in the view on the right. Now answer the question on the presentation slide...
7. Open *Finding the Length of the Day* in the *Trigonometry Problems* chapter and follow the on-screen instructions...
- a. Slide the slider until you find an appropriate view.
 - b. What information do you need to determine the time elapsed between sunrise and sunset?
 - c. Draw and label a suitable diagram to find an expression for A in terms of θ and α . Go back to the previous applet if it is more helpful.
 - d. Use your expression for A to determine Δt , the difference in times between sunset and sunrise for a given value of T.
8. Open *Finding the Polar Tilt in the Sun's Direction* in the same folder. Move the black spot labelled "N".
- a. What does it represent?
 - b. What does θ represent?
 - c. What do you think Ω represents? What is its value?
 - d. Slide the sliders until you find a view most useful to you. How does this diagram help you find out how θ it depends on T?
 - e. Draw and label a suitable diagram and have a go at deriving a formula for $\theta(T)$
9. Open <https://www.geogebra.org/m/xtfhmumb>. This is GeoGebra's 3D software. Click on and experiment with the shapes by dragging –
- a. what does it tell you about the intersection of a plane and the centre of a sphere?
 - b. can you input an equation of a plane that intersects the sphere without going through its centre? What would this tell you about such intersections?
10. Now open *Earth 3D Simulation (Using 2D Equations)* in the same folder and experiment with the sliders. Ensure you are fully familiar with the effects of T, t and α .

Which Capital City?

11. In the GeoGebra app on your desktop, create a slider for α – think about the values it can have and enter in the relevant information.
12. Enter a suitable expression for y in terms of x that will show how Δt varies with T for a given value of α . Remember the roles of $\theta(T)$ and Ω in formulating your expression.

13. Open the Excel file *Data to Dump into GeoGebra.xls*.
14. Select the Spreadsheet view in GeoGebra.
15. Copy and paste the Excel data into the first two columns.
16. In the third column, write “=(A1,A2)” and see what happens.
17. Click and drag this formula down to the end of the list, then select the whole column, right-click and uncheck “show label”
18. These are the data for a capital city somewhere on Earth. Using your graph (and Google!), can you suggest which city/cities these data come from?