



## Task 12 Largest Cylinder Inscribed in a Cone

- Open a new window (Ctrl+N). In the Graphics view, use the "Circle" tool to draw a 1. circle centred at the origin and passes through (1,0).
- Activate the 3D Graphics view. Use the Extrude to Pyramid or Cone tool 1 in the 2.

toolbox. Drag up the circle to create a cone of height 2. Use the Point tool  $||_{\bullet}^{A}$ to create the apex C of the cone.

- Close the Graphics view and activate the Graphics 2 view. In Graphics 2 view create a slider e 3. of value from 0 to 1 with increment 0.01.
- Create a point D which moves on the altitude of the cone by entering: 4. (0, 0, e z(C))
- in the toolbox, click on D and the z-Axis to Use the Perpendicular Plane tool 5. create a plane **f** through D perpendicular to the *z*-Axis.
- Use the Intersect Two Surfaces tool (A), click on the plane **f** and the cone **a** to create the 6. intersection curve of the cone and the plane. Hide the plane **f**.
- Use the Point tool  $\| \bullet^{\mathsf{A}} \|$ to create a point E on the intersection curve. Enter: 7.
  - r = Distance[D, E]
- Use the Cylinder tool [] in the [] toolbox. Click on A, D and enter **r** to create the 8. cylinder **h** inscribed in the cone. Make the cone more transparent. Hide the axe and the points.
- Click on Graphics 2 view. In the input bar enter: 9. (z(D), h)

to create a movable point F to trace how the volume (h) varies against the height of the cylinder (z(D)).

10. Use the Locus tool  $\bigwedge$  in the toolbox  $\square$ . Click on the movable point F and the slider e to construct the locus of F when e varies. Change the style of F as "×" and label

Colour F and the curve in red.

11. Drag the slider to investigate when the cylinder inscribed in the cone would be largest.

it by its value.



Graphics 2

1.5

0.5

- 0 5

Sign ir

(0.66, 0.93)

= 0.33

File Edit View Options Tools Window Help

Algebra

Cone a: 2.09

Conic

o c: x<sup>2</sup>  $+ v^2 = 1$ 

Locus Ioc1 = Locus[F

Numbe

Input:

d: (0, 0, 2) q(t) = (0, 0, 0.66

k(t) = (0, 0, 0) +

p(t) = (0, 0, 0.66) Cylinder h: 0.93

3D Graphics