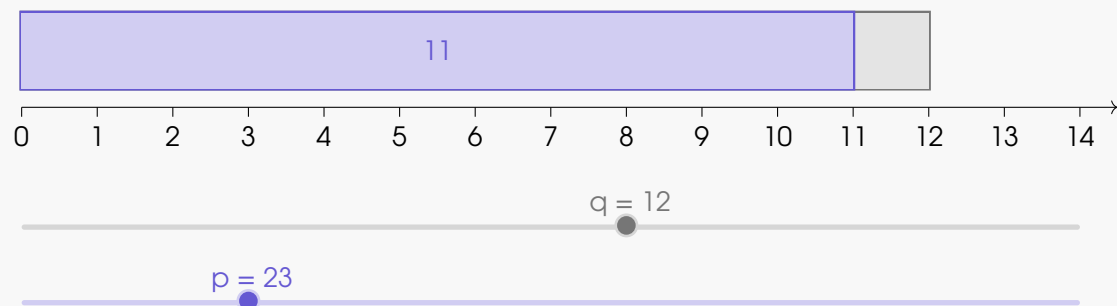


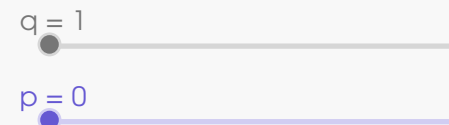
**Objective:** To create an applet that demonstrates the modulo operator.

**Mini-Objective 1:** To create sliders for integers  $p$  and  $q$ .

$$23 \pmod{12} = 11$$



$$p \pmod{q}$$



**Step 1:** Create a slider for  $p$ , such that  $p$  is an integer value from 0 to 100.

**Step 2:** Create a slider for  $q$ , such that  $q$  is an integer value from 1 to 20.

**Mini-Objective 2:** To represent the modulus as a fractional part of  $q$ .

**Slider**

Name  
p = 0

Number     Angle     Integer

| Interval | Slider     | Animation |
|----------|------------|-----------|
| Min      | Max        | Increment |
| <u>0</u> | <u>100</u> | <u>1</u>  |

CANCEL    **OK**

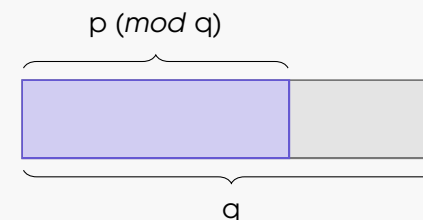
**Slider**

Name  
q = 1

Number     Angle     Integer

| Interval | Slider    | Animation |
|----------|-----------|-----------|
| Min      | Max       | Increment |
| <u>1</u> | <u>20</u> | <u>1</u>  |

CANCEL    **OK**



**Note:** If  $q = 0$ , then  $p \pmod{q}$  is undefined. Therefore,  $q$  must be greater than or equal to 1.

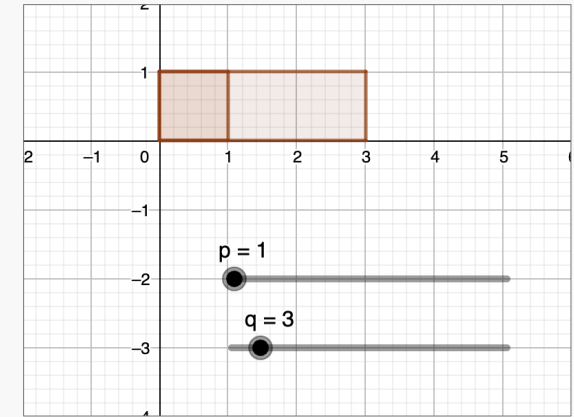
**Step 3:** Inside of the algebra window, define the following six points. In object settings, indicate points A and D as a fixed object

|   |           |   |
|---|-----------|---|
| + | A = (0,0) | ⋮ |
|   | → = (0,0) |   |
| + | B = (q,0) | ⋮ |
|   | → = (1,0) |   |
| + | C = (q,1) | ⋮ |
|   | → = (1,1) |   |

|   |                  |   |
|---|------------------|---|
| + | D = (0,1)        | ⋮ |
|   | → = (0,1)        |   |
| + | E = (Mod(p,q),1) | ⋮ |
|   | → = (1,1)        |   |
| + | F = (Mod(p,q),0) | ⋮ |
|   | → = (1,0)        |   |

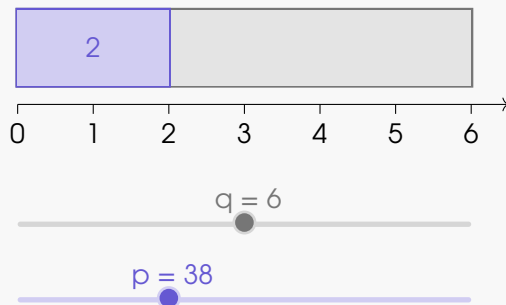
**Tip:** To access object setting, right-click on an object and then select settings.

**Step 4:** Select the Polygon tool. To represent  $p \pmod q$ , select points A → B → C → D → A. To represent  $q$ , select points A → D → E → F → A. Hide all points.

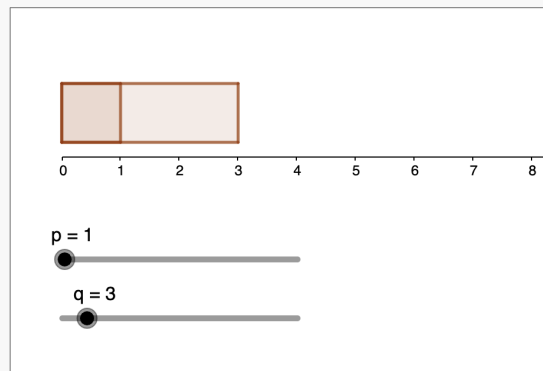


**Mini-Objective 3:** To add some final touches.

$$38 \pmod 6 = 2$$



**Step 5:** In graphics settings, hide the grid and y-axis. Show the x-axis in the positive direction only and have the x-axis cross at  $y = -0.25$



**Tip:** To access graphics settings, right-click on the graphics window and then select, Graphics.

**Step 6:** Select the Text tool to create a label that provides the value of  $p \pmod q$ .

**Text**

**B** / **Serif** **LaTeX formula**

$p \pmod q = \text{Mod}(p, q)$

▶ **Advanced**

CANCEL **OK**

**Tip:** To provide the value of an object, select the advanced drop-down, navigate to the objects tab and select empty box.

Step 7: Customize the appearance to your liking.

