Grades 5-8 (A), 9 (S)

Duration: 45 min
Tools: one piece / student, paper, scissors

Individual work
Keywords: Geometry, Similarity

507 - Build it from Paper


MATHS / TRANSFORMATION

## DESCRIPTION

Each student selects a Logifaces piece.
LEVEL 1 Students enlarge and reduce the size of the original piece using the standard units. They calculate the measurements for objects with the following scale factors: $2,10,20$ and $1 / 2$.

LEVEL 2 Students calculate the surface area and the volume of the pieces with scale factor 2 and $1 / 2$.
LEVEL 3 Students build a model of an enlarged or reduced piece using paper.
SOLUTIONS / EXAMPLES
LEVEL 1 :
Solution for block 112, using the notations of the figure below:


|  | $a$ | $b$ | $h_{1}$ | $h_{2}$ |
| :--- | :--- | :--- | :--- | :--- |
| Block 112: | 4 | $\sqrt{17}$ | 1 | 2 |
| Scale factor 2: | 8 | $2 \sqrt{17}$ | 2 | 4 |
| Scale factor 10: | 40 | $10 \sqrt{17}$ | 10 | 20 |
| Scale factor 20: | 80 | $\frac{1}{2} \sqrt{17}$ | $\frac{1}{2}$ | 40 |
| Scale factor $\frac{1}{2}$ | 2 |  | 1 |  |


| LEVEL 2 |  |  |
| :--- | :--- | :--- |
| Triangles | Base | Top |
|  |  |  |
| Block 112: | $A=4 \sqrt{3}$ | $A=2 \sqrt{13}$ |
| Scale factor 2: | $A=\left(\frac{1}{2}\right)^{2} \times 4 \sqrt{3}$ | $A=2^{2} \times 2 \sqrt{13}$ |
| Scale factor $\frac{1}{2}:$ |  |  |

Side faces

|  |  |  |
| :--- | :--- | :--- |
| Block 112: | $A=6$ | $A=4$ |
| Scale factor 2: | $A=2^{2} \times 6$ | $A=2^{2} \times 4$ |
| Scale factor $\frac{1}{2}:$ | $A=\left(\frac{1}{2}\right)^{2} \times 6$ | $A=\left(\frac{1}{2}\right)^{2} \times 4$ |


|  | Surface area | Volume |
| :--- | :--- | :--- |
| Block 112: | Surface $=16+4 \sqrt{3}+2 \sqrt{13} \approx 30.14$ | Volume $=\frac{4}{3} \times 4 \sqrt{3}$ |
| Scale factor 2: | Surface $=2^{2} \times(16+4 \sqrt{3}+2 \sqrt{13}) \approx 120.56$ | Volume $=2^{3} \times \frac{4}{3} \times 4 \sqrt{3}$ |
| Scale factor $\frac{1}{2}:$ | Surface $=\left(\frac{1}{2}\right)^{2} \times(16+4 \sqrt{3}+2 \sqrt{13}) \approx 120.56$ | Volume $=\left(\frac{1}{2}\right)^{3} \times \frac{4}{3} \times 4 \sqrt{3}$ |

## LEVEL 3

PRIOR KNOWLEDGE
Similarity
RECOMMENDATIONS / COMMENTS
This exercise can be used to practise the concept of similarity. It is recommended to see exercises $\underline{513 \text { - Surface }}$ Area Calculation and 517 - Heights and Volumes first.

